

$$(1) \quad A, \quad 0 \leq P(A) \leq 1$$

$$A^c, \quad P(A^c) = 1 - P(A)$$

$$P(X > 3) = 1 - P(X \leq 3)$$

$$(2) \quad A, B$$

$$A \cap B$$

$$A \cup B$$

$$1^\circ P(A \cap B)$$

- ① disjoint? $P(A \cap B) = 0$
- ② independent? $P(A \cap B) = P(A)P(B)$
- ③ do we know $P(A)$ and $P(A \cap B^c)$?
 $P(A \cap B) = P(A) - P(A \cap B^c)$
- ④ do we know $P(A)$ and $P(B)$ and $P(A \cup B)$?
 $P(A \cap B) = P(A) + P(B) - P(A \cup B)$
- ⑤ do we know the conditional probs?
 $P(A \cap B) = P(A) \cdot P(B|A) = P(B) \cdot P(A|B)$

2° $P(A \cup B)$

① disjoint? $P(A \cup B) = P(A) + P(B)$

② independent? $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
 $= P(A) + P(B) - P(A) \cdot P(B)$

③ $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

(3) conditional prob

$P(A|B)$

1° def: $P(A|B) = \frac{P(A \cap B)}{P(B)}$
(if we know $P(B)$)

2° if we don't know $P(B)$, but we know $P(A^c \cap B)$

then, $P(B) = P(A \cap B) + P(A^c \cap B)$

so $P(A|B) = \frac{P(A \cap B)}{P(A \cap B) + P(A^c \cap B)}$

3° $P(A \cap B) = P(A)P(B|A) = P(B) \cdot P(A|B)$

$$P(A|B) = \frac{P(A)P(B|A)}{P(B)}$$